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Optic Flow-Based Nonlinear Control and Sub-optimal Guidance for Lunar Landing

Guillaume Sabiron^{1,2}, Laurent Burlion², Thibaut Raharijaona¹, and Franck Ruffier¹

Abstract—A sub-optimal guidance and nonlinear control scheme based on Optic Flow (OF) cues ensuring soft lunar landing using two minimalistic bio-inspired visual motion sensors is presented here. Unlike most previous approaches, which rely on state estimation techniques and multiple sensor fusion methods, the guidance and control strategy presented here is based on the sole knowledge of a minimum sensor suite (including OF sensors and an IMU). Two different tasks are addressed in this paper: the first one focuses on the computation of an optimal trajectory and the associated control sequences, and the second one focuses on the design and theoretical stability analysis of the closed loop using only OF and IMU measurements as feedback information. Simulations performed on a lunar landing scenario confirm the excellent performances and the robustness to initial uncertainties of the present guidance and control strategy.

I. INTRODUCTION

During the last few decades, increasing attention has been paid to autonomous planetary landing, especially small lander applications requiring few resources for use in situations where mass, size and low-consumption embedded devices are of crucial importance. Applications of this kind always require a Guidance Navigation and Control (GNC) algorithm and finely tuned sensors which are able to bring the lander gently onto the ground. Minimalistic vision based systems equipped with lightweight bio-inspired sensors providing rich sensory feedback are particularly suitable for this purpose. Many authors have used vision based systems for various applications such as terrain relative navigation (see [1]), automatic landing, 3-D environment mapping and hazard avoidance. However, in most of these recent developments, a high computational cost is associated with the image processing algorithm extracting visual cues from the onboard cameras' output.

Bio-inspired devices have provided interesting solutions based on the Optic Flow (OF) cues which convey information about the relative velocity and the proximity of obstacles. The OF has been used in several studies to perform hazardous tasks such as taking off, terrain-following, and landing safely and efficiently by mimicking insects' behavior (see

[2], [3]), avoiding frontal obstacles (see [4]–[7]), tracking a moving target (see [8]) and hovering and landing on a moving platform (see [9]). We previously tested a miniature 2.8 g 6-pixel OF sensor implemented on a 80 kg helicopter by flying it outdoors over various fields, with promising results [10].

OF based lunar landing has been addressed in several studies using either a nonlinear observer coupled to a Linear Quadratic (LQ) controller to track a constant OF reference in [11] or Proportional Integral Derivative (PID) type controllers to track a constant OF reference in [12], and more recently, using a Model Predictive Control approach in [13]. After presenting theoretical results on OF based optimal control in [14], previous authors adopted an OF reference signal based on the expansion OF (an index to the vertical velocity divided by the height) which was no longer constant, but decreased constantly or exponentially (see [15]).

In the present study, trajectory tracking was performed using a precomputed fuel-optimal trajectory assessed via nonlinear programming methods in order to avoid the unnecessary fuel expenditure liable to occur when following constant bio-inspired OF reference signals. In the control laws adopted, a rigorous Lyapunov approach was used to ensure the global stability and convergence of the closed loop including two nonlinear controllers based on translational and expansional OF measurements.

This paper is structured as follows. In section II, the dynamic model for the lander and the mathematical definition of the OF are presented. Section III describes the scenario studied and discusses the sub-optimal guidance scheme. Section IV presents the control strategy used for OF tracking purposes. Section V gives the results of the numerical simulations performed. Lastly, section VI contains some concluding comments and outlines our forthcoming projects.

II. LUNAR LANDER DYNAMIC MODELING AND OPTIC FLOW EQUATIONS

In this section, the dynamic model for the system presented in Fig. 2 and the mathematical background to OF studies are described. The autopilot presented here consists of an OF-based control system operating in the vertical plane (\vec{e}_x, \vec{e}_z) (2-D position plus 1-D attitude), which controls the spacecraft's main thruster force and pitch angle. To stabilize the lander, it is necessary to cope with nonlinearities and the inherent instability of the system. Since the lunar atmosphere is very thin, no friction or wind forces are applied here to the

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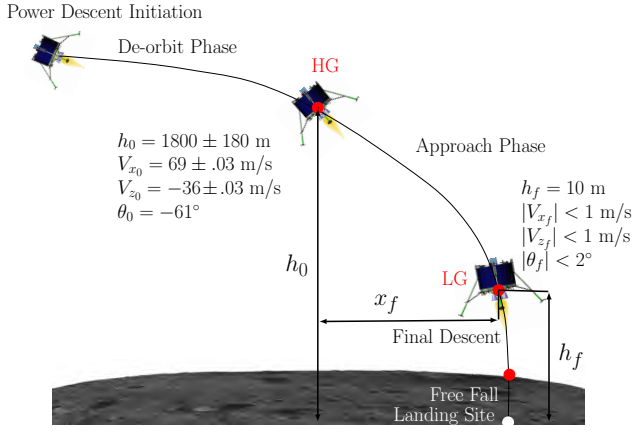


Fig. 2. The lander's objectives are to reach LG (10 m high) with both vertical and horizontal velocities of less than 1 m/s in absolute values and a pitch angle in the $\pm 2^\circ$ range. Adapted from [16].

* indicates the optimality in terms of the mass, i.e., the fuel consumption). In this paper, optimality refers to the outputs of the optimization problem (u_{th}^* , u_θ^*) and the associated reference trajectory (\dot{V}_x^* , \dot{V}_z^* , V_x^* , V_z^* , h^* , θ^*). Looking for the least fuel-consuming trajectory is equivalent to finding the control sequence u^* that minimizes the use of the control signal (see (1f)). The optimization problem can then be expressed as follows:

Solve

$$\min_{u_{th}(t), u_\theta(t)} \int_{t_0}^{t_f} (u_{th}(t) + |u_\theta(t)|) dt \quad (7)$$

Subject to

Equations (1a)-(1f)

$$\begin{cases} V_z(t_0) = -36 \text{ m/s}, & |V_{zf}| < 1 \text{ m/s} \\ V_x(t_0) = 69 \text{ m/s}, & |V_{xf}| < 1 \text{ m/s} \\ h(t_0) = 1800 \text{ m}, & h_f = 10 \text{ m} \\ \theta(t_0) = -61^\circ, & |\theta_f| < 2^\circ \end{cases} \quad (8)$$

$$\begin{cases} 0 < u_{th} < 3438 \text{ N} \\ -44 < u_{pitch} < 44 \text{ N} & \forall t \in [t_0, t_f] \\ (-V_z, V_x, h, x) > 0 \\ |\dot{\theta}| < 1.5^\circ/\text{s} \end{cases} \quad (9)$$

This offline sub-optimal guidance strategy was implemented using Matlab optimization software on the nonlinear system under constraints to bring the system from HG to LG. To solve this continuous time optimization problem, many freely available Matlab toolboxes based on various methods can be used. The solution provided by ICLOCS (Imperial College London Optimal Control Software, [20]) based on the IPOPT solver suited our needs for the numerical implementation of a nonlinear optimization problem in the case of the continuous system subjected to boundary and state constraints using the interior point method. The simulation of the open loop under optimal control was therefore run on the nonlinear system to assess the optimal OF and pitch profiles (ω_x^* , ω_z^* , θ^*).

Equation (1a)-(1f) describes the dynamic lander, (8) gives the initial and final conditions and (9) gives the actuator and system constraints imposed along the trajectory. For safety reasons, a 10% margin was added to the thrusters' physical saturation in order to give the lander greater maneuverability around the predefined trajectory at any point. It is worth noting that a terminal constraint could easily be added if required to the downrange x to make pinpoint landing possible, but this might greatly increase the fuel consumption. Since the case may arise where $\dot{\theta} = -\omega_R > \omega_T$ and thus $\omega_{measured} < 0$, we had to use a bi-directional version of the 6-pixel VMS adapted for use in the following measurement range: $\omega_{measured} \in [-20^\circ/\text{s}; -0, 1^\circ/\text{s}] \cup [0, 1^\circ/\text{s}; 20^\circ/\text{s}]$. The fuel expenditure decreases the lander's mass by Δm , which is defined as the difference between the initial and final mass of the lander $\Delta m = m_{ldr0} - m_{ldr}(t_f)$ where $m_{ldr0} = 762 \text{ kg}$ and

$$m_{ldr}(t_f) = m_{ldr}(t_0) - \frac{1}{g_{Earth}} \int_{t_0}^{t_f} \left(\frac{u_{th}(\epsilon)}{I_{spth}} + \frac{|u_\theta(\epsilon)|}{I_{sp\theta}} \right) d\epsilon \quad (10)$$

In order to make sure that the sum $\omega_{grd-trh} = \omega_T + \omega_R$ does not cancel itself out (i.e. $\omega_T = -\omega_R$), the pitch rate ($\omega_R = \dot{\theta}$) was constrained as follows: $|\dot{\theta}| = |\omega_R| < 1.5^\circ/\text{s}$. Under all these conditions, the optimal control sequences (u_{th}^* , u_θ^*) were processed: the optimal solution was obtained with $t_f = 51.46\text{s}$ and a mass change of $\Delta m < 33.6 \text{ kg}$ (amounting to 4.4% of the initial mass). The trajectory modeled under these constraints can be said to be optimal in the case of a more highly constrained problem. Additional constraints were imposed on $\dot{\theta}$ and the 10% margin on the thrust to account for the sensors' and actuators' operating ranges, resulting in a more highly constrained problem than the system can actually deal with. In any case, both of these constraints (the saturated pitch rate and the 10% margin added to the thrust) resulted in very similar fuel expenditure predictions to that obtained without these additional constraints (amounting to a difference of only 0.21%).

IV. LYAPUNOV-BASED NONLINEAR CONTROL DESIGN

In this section, a control design ensuring soft lunar landing based on the knowledge of the OF and IMU measurements is presented. The control problem to be solved here focuses on the tracking of translational and expansional OF reference signals. In particular, two control signals are computed, one for the horizontal thrust u_x and one for the vertical thrust u_z . Both u_x and u_z are then fused into a jointly delivered control signal $u_{th} = \sqrt{u_x^2 + u_z^2}$.

A. Height boundedness

Here we look for a time varying bound on the height h From:

$$\omega_z = \frac{V_z}{h} = \frac{d}{dt} \ln(h) \quad (11)$$

we have

$$\int_{t_0}^t \omega_z(s) ds = \ln \left(\frac{h(t)}{h(t_0)} \right) \quad (12)$$

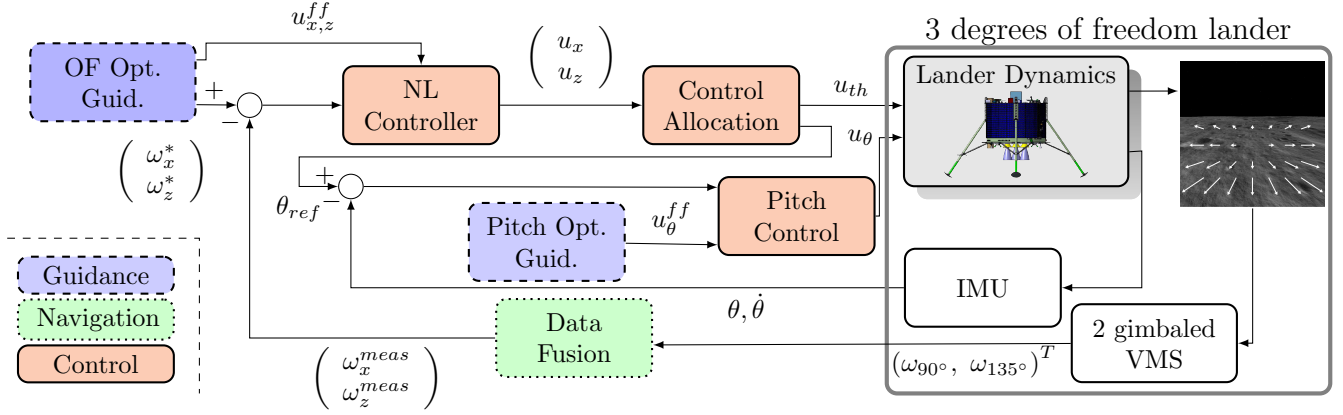


Fig. 3. Sketch of the full GNC solution. The dynamic model for the lander with 2×6 -pixels VMS feeding the data fusion block along with an IMU. The data fusion block estimates high interest OF values, which are conveyed to the nonlinear controller. The control allocation block transforms the control signal into a braking force defining the magnitude of the thrust vector and a reference pitch angle. The inner attitude control loop delivers the torque control signal u_θ assessed via the linear output feedback controller and a sub-optimal guidance strategy defining the feedforward term (corresponding to $u_x^{ff} = \dot{V}_x^*$ and $u_z^{ff} = \dot{V}_z^*$ in the control law equations). Adapted from [16].

which gives

$$h(t) = h(t_0) e^{\int_{t_0}^t \omega_z(s) ds} \quad (13)$$

where $\omega_z(t) < 0$ and $h(t) > 0$. Since it can be deduced from the initial conditions that $h(t_0) \in [1620, 1980]$, from (13) it is thus possible to compute time-varying bounds on the height such that $\forall t \geq t_0$ $h(t) \in [h_{min}(t), h_{max}(t)]$ where:

$$\begin{cases} h_{min}(t) = 1620 e^{\int_{t_0}^t \omega_z(s) ds} \\ h_{max}(t) = 1980 e^{\int_{t_0}^t \omega_z(s) ds} \end{cases} \quad (14)$$

which means that at each time step, an upper and a lower bound on $h(t)$ depending on the uncertainty at HG are known.

Remark If the measurement $\omega_z^{meas}(s)$ is corrupted with noise i.e. $\omega_z^{meas}(s) - d \leq \omega_z(s) < \omega_z^{meas}(s) + d < 0$ where $d \geq 0$ then

$$\begin{cases} h_{min}(t) = 1620 e^{\int_{t_0}^t \omega_z^{meas}(s) - d ds} \\ h_{max}(t) = 1980 e^{\int_{t_0}^t \omega_z^{meas}(s) + d ds} \end{cases}$$

B. Z dynamics

The nonlinear control design is achieved using the following Lyapunov function candidate \mathcal{L}_1 so that (see [21]):

$$\mathcal{L}_1 = \frac{1}{2} S_z^2 \quad (15)$$

where S_z is defined such as $S_z = \omega_z - \omega_z^*$.

Its corresponding time derivative might therefore be expressed as follows:

$$\dot{\mathcal{L}}_1 = S_z \left[\frac{\dot{V}_z}{h} - \frac{\dot{V}_z^*}{h^*} - \omega_z^2 + \omega_z^{*2} \right] \quad (16)$$

$$\dot{\mathcal{L}}_1 = S_z \left[\frac{\dot{V}_z - \dot{V}_z^*}{h} + \dot{V}_z^* \left(\frac{1}{h} - \frac{1}{h^*} \right) - S_z^2 - 2\omega_z^* S_z \right] \quad (17)$$

Two possible cases then arise, depending on the sign of S_z .

A sign study of S_z gives:

- When $S_z > 0$

$$\dot{\mathcal{L}}_1 < S_z \left[\frac{\dot{V}_z - \dot{V}_z^*}{h} + \dot{V}_z^* \left(\frac{1}{h} - \frac{1}{h^*} \right) - 2\omega_z^* S_z \right] \quad (18)$$

where $h > 0$ in the reference scenario under consideration, using bounds on $h(t)$ such that:

$$\frac{1}{h_{max}(t)} - \frac{1}{h^*(t)} \leq \left(\frac{1}{h(t)} - \frac{1}{h^*(t)} \right) \leq \frac{1}{h_{min}(t)} - \frac{1}{h^*(t)} \quad (19)$$

This gives

$$\dot{\mathcal{L}}_1 \leq S_z \left(\frac{\dot{V}_z - \dot{V}_z^*}{h} \right) + |S_z| |\dot{V}_z^*| h_{bound} + |2\omega_z^*| S_z^2 \quad (20)$$

where

$$h_{bound} = \max \left(\left| \frac{1}{h_{max}(t)} - \frac{1}{h^*} \right|, \left| \frac{1}{h_{min}(t)} - \frac{1}{h^*} \right| \right) \quad (21)$$

We now need to find a control signal satisfying $\dot{\mathcal{L}}_1 < 0$. The virtual control signal u_z features in the dynamic model for the lander in the form of $\dot{V}_z = \frac{u_z}{m} - g_{Moon}$, where $u_z = \cos(\theta) u_{th}$. We take:

$$u_z(t) = m \left(\dot{V}_z^* - k_a(t) S_z - k_b(t) \text{sgn}(S_z) + g_{Moon} \right) \quad (22)$$

$$\text{where } \text{sgn}(X) = \begin{cases} 1 & X \geq 0 \\ -1 & X < 0 \end{cases}$$

We obtain

$$\dot{\mathcal{L}}_1 \leq S_z^2 \left(\frac{-k_a(t)}{h} + |2\omega_z^*| \right) + |S_z| \left(\frac{-k_b(t)}{h} + |\dot{V}_z^*| h_{bound} \right) \quad (23)$$

Lastly, we take the gains $k_a(t)$ and $k_b(t) \forall t \geq 0$:

$$k_a(t) > h_{max}(t) |2\omega_z^*(t)| \quad (24)$$

$$k_b(t) > h_{max}(t) |\dot{V}_z^*(t)| h_{bound} \quad (25)$$

so that $\dot{\mathcal{L}}_1 < 0$.

- When $S_z < 0$

From equation (17), one can obtain

$$\dot{\mathcal{L}}_1 \leq S_z \left(\frac{\dot{V}_z - \dot{V}_z^*}{h} \right) + |S_z| |\dot{V}_z^*| h_{bound} + |2\omega_z^*| S_z^2 - S_z^3 \quad (26)$$

We now need to find a control signal satisfying $\dot{\mathcal{L}}_1 < 0$
We take:

$$u_z(t) = m \left(\dot{V}_z^* - k_a(t) S_z - k_b(t) \text{sgn}(S_z) - k_c(t) S_z^2 + g_{Moon} \right) \quad (27)$$

Hence

$$\begin{aligned} \dot{\mathcal{L}}_1 \leq & S_z \left(\frac{-k_a(t) S_z - k_b(t) \text{sgn}(S_z) - k_c(t) S_z^2}{h} \right) \\ & + |S_z| |\dot{V}_z^*| h_{bound} + |2\omega_z^*| S_z^2 - S_z^3 \end{aligned} \quad (28)$$

$$\begin{aligned} \dot{\mathcal{L}}_1 \leq & S_z^2 \left(\frac{-k_a(t)}{h} + |2\omega_z^*| \right) \\ & + |S_z| \left(\frac{-k_b(t)}{h} + |\dot{V}_z^*| h_{bound} \right) \\ & - S_z^3 \left(1 + \frac{k_c(t)}{h} \right) \end{aligned} \quad (29)$$

where we choose the gain $k_c(t) \forall t \geq 0$ so that:

$$k_c(t) < -h_{max}(t) \quad (30)$$

and $k_a(t)$, $k_b(t)$ such as (29-29) are ensured.

Therefore $\dot{\mathcal{L}}_1 < 0$, which means that \mathcal{L}_1 tends asymptotically toward 0 (since $\mathcal{L}_1 > 0$), and lastly, (15) ensures that $\omega_z \rightarrow \omega_z^*$ asymptotically.

Let us now combine all the expressions for the control signal, with (22-27) to obtain the unified control signal equation:

$$\begin{aligned} u_z(t) = & m \left(\dot{V}_z^* - k_a(t) S_z - k_b(t) \text{sgn}(S_z) \right. \\ & \left. - \left(\frac{1 - \text{sgn}(S_z)}{2} \right) k_c(t) S_z^2 + g_{Moon} \right) \end{aligned} \quad (31)$$

C. X dynamics

A similar Lyapunov function based approach is used on the X dynamics:

Let us define S_x as $S_x = \omega_x - \omega_x^*$:

$$\mathcal{L}_2 = \frac{1}{2} S_x^2 \quad (32)$$

$$\dot{\mathcal{L}}_2 = S_x \left[\frac{\dot{V}_x}{h} - \frac{\dot{V}_x^*}{h^*} - \omega_x \omega_z + \omega_x^* \omega_z^* \right] \quad (33)$$

One can say that:

$$\dot{\mathcal{L}}_2 < S_x \left[\frac{\dot{V}_x - \dot{V}_x^*}{h} + \dot{V}_x^* \left(\frac{1}{h} - \frac{1}{h^*} \right) + \omega_x \omega_z + \omega_x^* \omega_z^* \right] \quad (34)$$

with $h > 0$ in the reference scenario adopted:

$$\frac{1}{h_{max}(t)} - \frac{1}{h^*} \leq \left(\frac{1}{h} - \frac{1}{h^*} \right) \leq \frac{1}{h_{min}(t)} - \frac{1}{h^*} \quad (35)$$

This gives:

$$\dot{\mathcal{L}}_2 \leq S_x \left(\frac{\dot{V}_x - \dot{V}_x^*}{h} \right) + \left[|\dot{V}_x^*| h_{bound} + |\omega_x \omega_z + \omega_x^* \omega_z^*| \right] |S_x| \quad (36)$$

where h_{bound} as defined in (21).

We need to find a control signal that ensure $\dot{\mathcal{L}}_2 < 0$. The virtual control signal u_x features in the dynamic model for the lander in the form of $\dot{V}_x = \frac{u_x}{m}$, where $u_x = \sin(\theta) u_{th}$. We choose:

$$u_x(t) = m \left(\dot{V}_x^* - k_a(t) \text{sgn}(S_x) - k_b S_x \right) \quad (37)$$

where $\forall t \geq 0$

$$k_a(t) > h_{max}(t) \left[|\dot{V}_x^*| h_{bound} + |\omega_x \omega_z + \omega_x^* \omega_z^*| \right] \quad (38)$$

thus with $\dot{\mathcal{L}}_2 < -k_b S_x$, we choose a relatively small $k_b > 0$ to prevent any chattering of S at values around zero.

Finally, $\dot{\mathcal{L}}_2 < 0$, which means that \mathcal{L}_2 tends asymptotically toward 0 (since $\mathcal{L}_2 > 0$), and lastly, (32) ensures that $\omega_x \rightarrow \omega_x^*$ asymptotically.

D. Pitch control law

To control the attitude, a proportional derivative controller drives the spacecraft's pitch (via the inner loop), which gives faster dynamics in the inner loop than on an outer loop:

$$u_\theta(t) = u_\theta^{ff}(t) + K_p \varepsilon_\theta(t) + K_d \frac{d}{dt} \varepsilon_\theta(t) \quad (39)$$

where $u_\theta^{ff}(t)$ corresponds to the optimal control sequence $u_\theta^*(t)$ computed with the mass-optimal trajectory and $\varepsilon_\theta(t) = \theta_{meas}(t) - \theta_{ref}(t)$. The reference signal θ_{ref} is based on the two virtual control signals u_x and u_z , so that:

$$\theta_{ref} = \arctan \left(\frac{u_x}{u_z + \varepsilon} \right) \quad (40)$$

where ε is taken to be very small to avoid having to divide by zero.

V. SIMULATION RESULTS

Once the optimal trajectory has been defined, the OF and pitch profiles (ω_x^* , ω_z^* , θ^*) as well as the optimal feedforward control signals \dot{V}_x^* and \dot{V}_z^* (see (27,37)) are available for implementation along with the control laws defined in (27), (37) and (39). Simulations were run on a Matlab/Simulink simulator taking the lander's dynamics, actuator dynamics (which were taken to be first order systems) and the saturation into account. Random noise was also added to the OF sensor model. In order to assess the robustness of the model to initial uncertainties, an initial height condition ($h(t_0)$) was taken to be in the $1800 \pm \delta_h$ range, where $\delta_h = 180$ m. The result of simulations in which $h(t_0)$ increased by 20 m after each run are presented in Fig. 4. As can be seen from this figure, which presents the trajectory in the 2-D plane and the final velocities, pitch angle and fuel consumption, our new G&C almost meets the tight specifications imposed. The final vertical velocity is slightly higher than the objective. The final pitch angle was in the $\pm 2^\circ$ range, the horizontal velocity was below 1 m/s, whereas the final vertical velocity was only 0.68 m/s above the objective (corresponding to a decrease in the speed of $100 \frac{V_{zf} - V_z(t_0)}{V_z^*(t_f) - V_z(t_0)} = 98\%$ of the tight requirements)

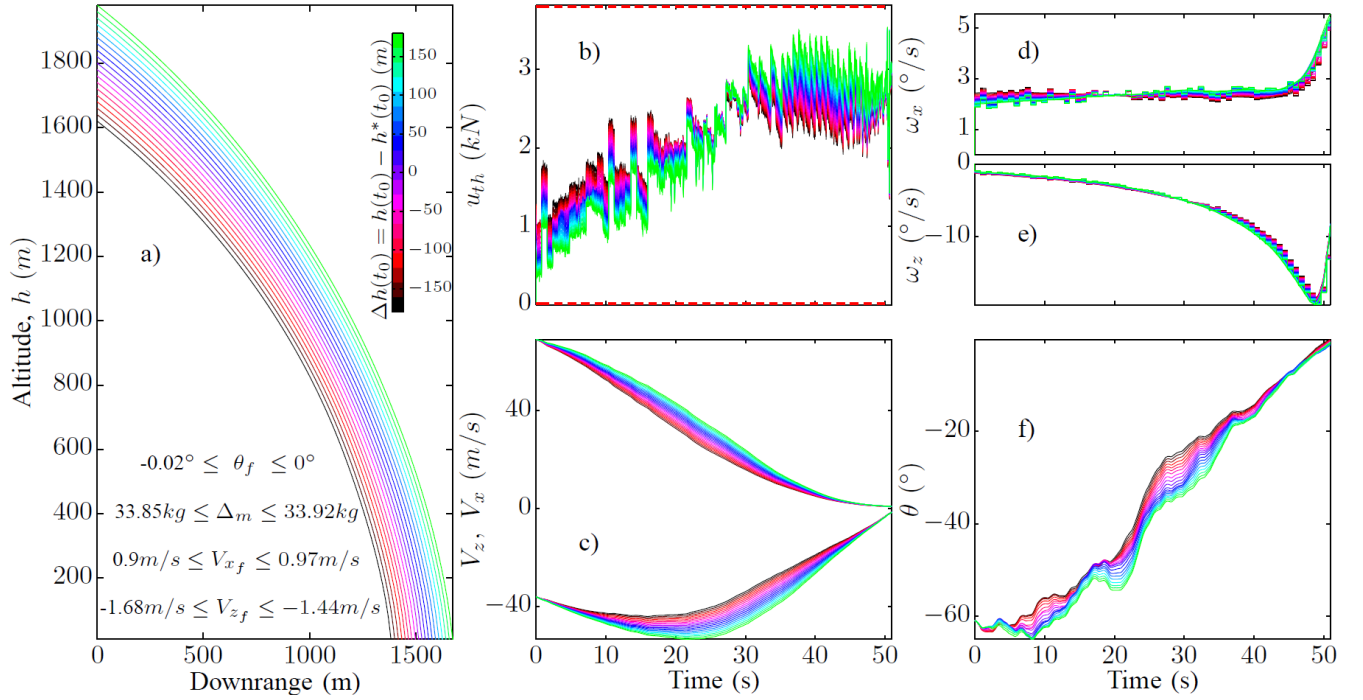


Fig. 4. Closed loop behavior from HG to LG in simulations with $h(t_0) \in [h_{min}(t_0), h_{max}(t_0)]$. a) Height h versus downrange x . b) Control sequence $u_{th} = \sqrt{u_x^2 + u_z^2}$. Saturation of the control signal u_{th} is defined in such a way that $0 \text{ N} \leq u_{th} \leq 3820 \text{ N}$. c) Velocities V_x, V_z . d) Measured OF and optimal reference OF profile (black dashed lines). e) Pitch trajectories corresponding to various initial heights.

in the worst simulated case. The fuel consumption was $\Delta m \leq 34.22 \text{ kg}$, although we observed that $\Delta m^* = 33.6 \text{ kg}$, which means that even when the initial height was far above the pre-computed optimal trajectory, the fuel consumption approached the optimal value very closely (it was only 1.2% higher) although the final constraints were almost met. It is worth noting that the control signal $u_{th}(t)$ presented in Fig. 4.b never reached the upper or lower saturation levels depicted in dashed red lines. The evolution of the velocities, which tended toward 1 m/s in absolute values, is presented in Fig. 4.c, whereas Fig. 4.d-e shows the evolution of the optic flow measured superimposed on the optimal reference signals. Noise was modeled based on previous results obtained on the real sensor, which showed the occurrence of a refresh rate of approximately 7 Hz and a standard deviation of the error of $0.4^\circ/\text{s}$. Lastly, Fig. 4.f presents the pitch evolution starting at $\theta(t_0) = -61^\circ$ and moving toward $-2^\circ \geq \theta_f \geq 2^\circ$ in the case of all the initial heights. In conclusion, the G&C strategy presented in this study can be said to be suitable for handling the approach phase during lunar landing, even in the presence of large initial uncertainties as far as the height is concerned.

VI. CONCLUSION

This paper presents a nonlinear soft lunar landing controller, in which optical flow measurements are used along with the IMU data. The originality of our approach lies in the fact that neither the linear velocity nor the distance from the target need to be determined. The present approach involves an image based visual control algorithm which

requires only 2×6 pixels and inertial data for performing the derotation of the flow. A rigorous analysis of the stability of the closed-loop systems presented here was conducted, which resulted in the design of sliding mode type control laws regulating the translational and expansional OF. Via nonlinear programming procedures, the optimal reference trajectory in terms of the fuel consumption was computed offline and used in the closed loop as feedforward terms for providing the OF and pitch control loops with reference signals. The guidance algorithm proposed here is designated as sub-optimal in terms of fuel expenditure since it provides the system with an optimal trajectory from the HG to the LG computed via nonlinear programming. The actual landing strategy is therefore sub-optimal since the optimal trajectory is computed offline only once. In view of the simulation results we can conclude that the strategy is close to the optimal behavior. Simulations with various initial conditions gave a clear picture of the performances of the present algorithm. The experimental results obtained confirmed that the G&C strategy developed here almost fulfilled the requirements in terms of the spacecraft's final position, velocity and fuel consumption. It is now proposed to conduct further research on the following lines. First, in order to do away with the use of bulky IMUs and gimbal systems, an observer based solely on the OF could be used to accurately estimate ω_x, ω_z and θ . An initial study on an observer of this kind was recently presented in [22]. Secondly, although the final pitch angle estimates meet the objectives, an improvement could be made by designing a nonlinear control law regulating the pitch dynamics in order to avoid having to differentiate the

pitch error, which depends on the control signals.

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